



# Einladung zum Oberseminar Mathematische Logik

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## Modal Logic over Ordinals

Modal Logic ML is a fragment of First-order logic known for its good model-theoretic and algorithmic properties. We will consider ML interpreted in ordinal models. These are structures with some unary predicates and a single binary relation which is a descending, well-founded, strict linear order  $>$  on the universe. Since every such order is isomorphic to an ordinal number, we call these models ordinal models. I will show that, assuming finiteness of the vocabulary, ML over ordinal models is compact. That is, if  $t$  is a set of ML formulae over finitely many symbols and every finite fragment of  $t$  has an ordinal model then so does the entire  $t$ . Both the result and the proof (using Higman's Lemma as its technical heart) are arguably surprising. If time permits, I will discuss how to use the facts established in the proof to easily reprove and strengthen the known soundness and (weak) completeness of modal axiomatization  $K4.3W$  with respect to the class of all ordinal models.

No knowledge of modal logic will be assumed.

Ort: Mathematik Ost, Seminarraum 01.003

Zeit: Montag, 06.05.2024 16:15

Zu diesem Vortrag laden wir Sie herzlich ein.

*gez. Anton Freund*