



# Oberseminar Mathematische Strömungsmechanik

Institut für Mathematik der Julius-Maximilians-Universität Würzburg

**Hyperbolic equations - structure preserving methods & other topics**

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## Sharp interface modelling of phase change in two-phase flow

### *Abstract:*

The numerical modelling of evaporation in a two-phase fluid is difficult within a continuum description because the equation of state is non-convex in the spinodal region. Approximating the phase transition as a discontinuity in a macroscopic description allows to introduce an additional wave - an evaporation wave - where appropriate jump conditions hold. The structure of the Riemann problem solution is preserved though we have four waves with three equations. By imposing jump conditions that satisfy a so-called kinetic relation, taking into account local thermodynamics and heat conduction at the interface, the non-physical states in the spinodal region can be avoided and a proper solution can be determined.

We apply this two-phase Riemann solution as well as an approximate two-phase Riemann solver within a sharp interface approximation based on a ghost fluid approach. We compare simulations for benchmark Riemann problems with phase change with results from molecular dynamics. A truncated and shifted Lennard-Jones potential in molecular dynamics allows long time and large space scale simulations to approach the macroscopic scales. A highly accurate deduced equation of state for the Euler equations establishes a one-to-one correspondence of the molecular dynamics and the continuum solutions.

### References

T. Hitz, M. Heinen, J. Vrabec, C.-D. Munz: Comparison of Macro- and Microscopic Solutions of the Riemann Problem I. Supercritical Shock Tube and Expansion into Vacuum, *J. Comput. Phys.* 402 (2020)

T. Hitz, S. Jöns, M. Heinen, J. Vrabec, C.-D. Munz: Comparison of Macro- and Microscopic Solutions of the Riemann Problem II. Two-phase Shock Tube, *J. Comput. Phys.* 429 (2021)

via Zoom video conference (request the Zoom link from [klingen@mathematik.uni-wuerzburg.de](mailto:klingen@mathematik.uni-wuerzburg.de))

Friday, May 14 at 3 pm CET

Zu diesem Vortrag sind Sie herzlich eingeladen.

gez. Christian Klingenberg