

## **Einladung zum Oberseminar** Wissenschaftliches Rechnen

Julius-Maximilians-Universität Würzburg Lehrstuhl für Wissenschaftliches Rechnen IX

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## $L^1$ -control cost and the finite-time turnpike property

The finite-time turnpike property is an extreme form of the turnpike property where the optimal state reaches a desired steady state after finite time. This steady state is in turn a solution of a static optimal control problem corresponding to the initial dynamic optimal control problem on a finite time interval [0, T].

This extreme situation can occur if the control cost is given by a non-smooth norm, for example with an  $L^1$ -norm control cost. Moreover, to enforce the convergence to a steady state, a tracking term should be a part of the objective functional. The situation is clearly related to exact penalization, which is only possible with non-smooth penalty term.

We show that even if the tracking term is differentiable, the non-smooth control cost can lead to a finite-time turnpike phenomenon. A strictly convex tracking term has the advantage that it can enforce uniqueness of the optimal control.

We also discuss the approximation of the non-smooth control cost by smoothing kernels. The theory shows that the finite-time turnpike property is lost. But with increasing smoothing parameter, it is approximated, which is illustrated in numerical results.

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Zu diesem Vortrag laden wir Sie herzlich ein. You are cordially invited to this lecture.

> gez. Prof. Dr. Alfio Borzì gez. Prof. Dr. Frank Werner